

Bellwork in Canvas (in quizzes)

Sec 1.5

Inverse Relations and Functions - switching the x and y

There are different ways to find the inverse of a function as well as determining if a function has an inverse.

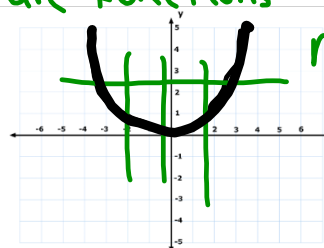
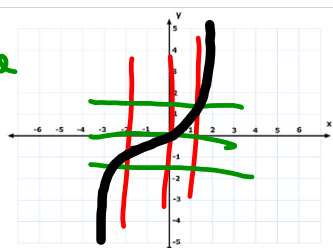
Remember the Vertical Line test? To determine if a graph has an inverse, we do a horizontal line test.

One to One - a function is said to be **one to one** if it passes **both** the vertical and horizontal line tests.

This means that the inverse is also a function

examples: do these graphs have an inverse? → which are functions

one to one



Finding the inverse of a function Algebraically

Inverse - switch the x and y
 $f^{-1}(x)$ means inverseexample: $f(x) = 2x + 5$

$$\begin{array}{lcl}
 y = 2x + 5 & & \text{Replace } f(x) \text{ with } y \\
 x = 2y + 5 & & \text{Switch the } x \text{ and } y \\
 \begin{array}{r} -5 \\ \hline x-5 = 2y \\ \hline \frac{x-5}{2} = y \end{array} & \left. \begin{array}{l} \\ \\ \end{array} \right\} & \text{Solve for } y \\
 f^{-1}(x) = \frac{x-5}{2} & & \text{Switch } y \text{ with } f^{-1}(x)
 \end{array}$$

Find the inverse of the functions.

example: $f(x) = \frac{x+3}{x-2}$

$$\begin{array}{lcl}
 \text{Replace } f(x) & & y = \frac{x+3}{x-2} \\
 \text{with } y & & \\
 \text{Switch } x & & \frac{x}{1} = \frac{y+3}{y-2} \\
 \text{and } y & & \\
 \left\{ \begin{array}{l} x(y-2) = 1(y+3) \\ xy - 2x = y + 3 \\ xy - y = 2x + 3 \\ \frac{y(x-1)}{x-1} = \frac{2x+3}{x-1} \\ y = \frac{2x+3}{x-1} \end{array} \right. & & \text{Solve for } y \\
 \text{Switch } y & & f^{-1}(x) = \frac{2x+3}{x-1} \\
 \text{for } f^{-1}(x) & &
 \end{array}$$

example: $h(x) = \sqrt{x+7}$

$$\begin{array}{lcl}
 y = \sqrt{x+7} & & \\
 x^2 = \sqrt{y+7}^2 & & \\
 x^2 = y + 7 & & \\
 \begin{array}{r} -7 \\ \hline x^2 - 7 = y \end{array} & & \\
 h^{-1}(x) = x^2 - 7 & &
 \end{array}$$

Verifying Inverse functions

- If two functions, $f(x)$ and $g(x)$, composites both equal x , then they are inverses.

$$f(g(x)) = g(f(x)) = x$$

ex. Verify that the two functions are inverses:

$$f(x) = 3x - 4$$

$$g(x) = \frac{x+4}{3}$$

$$f(g(x)) = \cancel{3} \left(\frac{x+4}{\cancel{3}} \right) - 4$$

$$x+4-4$$

$$x$$

$$g(f(x)) = \frac{3x - 4 + 4}{3} = \frac{3x}{3} = x$$

Because $f(g(x))$ and $g(f(x)) = x$ f and g are inverses