

Sec 5.4 Exponential Functions

THEOREM 5.12 INTEGRATION RULES FOR EXPONENTIAL FUNCTIONSLet u be a differentiable function of x .

$$1. \int e^x dx = e^x + C \quad 2. \int e^u du = e^u + C$$

$$\frac{1}{3} \int e^{3x+1} dx \quad u = 3x+1$$

$$du = 3 dx$$

$$\frac{1}{3} \int e^u du = e^u + C$$

$$= \frac{1}{3} e^{3x+1} + C$$

ex. $\int 5xe^{-x^2} dx$

$$-\frac{1}{2} \cdot 5 \int -2x e^{-x^2} dx$$

$$u = -x^2$$

$$du = -2x dx$$

$$-\frac{5}{2} \int e^u du$$

$$-\frac{5}{2} e^u + C = -\frac{5}{2} e^{-x^2} + C$$

$$= -\frac{5}{2} \left(\frac{1}{e^{x^2}} \right) + C = -\frac{5}{2e^{x^2}} + C$$

$$\begin{aligned} & \nearrow -(x)^2 \\ -x^2 & \neq (-x)^2 \\ e^{-x} & = \frac{1}{e^x} \\ e^{-x^2} & = \frac{1}{e^{x^2}} \end{aligned}$$

$$\int a^x dx = \left(\frac{1}{\ln a}\right)a^x + C$$

$$\text{ex. } \int 4^x dx = \frac{1}{\ln 4} 4^x + C = \frac{4^x}{\ln 4} + C$$

$$\begin{aligned} \text{ex. } \frac{1}{2} \int 6^{2x} dx & \quad \begin{array}{l} u = 2x \\ du = 2 dx \end{array} \\ \frac{1}{2} \int 6^u du &= \frac{1}{2} \left(\frac{1}{\ln 6}\right) 6^u + C = \frac{6^{2x}}{2 \ln 6} + C \\ &= \frac{6^{2x}}{\ln 36} + C \end{aligned}$$

Princeton book p. 335 7-12 all