

Bellwork - Khan Academy

Subject --> SAT --> Practice --> Math -->

Problem Solving and Data Analysis -->

**Scatterplots -->**

Practice - do 5 questions. Must show me,
this one I can't see from my side of program.



^{Sec 2.5}
Imaginary Roots come in pairs. Why?

$$\sqrt{x^2} = \sqrt{9}$$

$$x = \pm 3$$

$$\sqrt{x^2} = \sqrt{-4}$$

$$x = \pm 2i$$

So if one root is $a+bi$, the conjugate $a - bi$ is the matching root.

Find conjugate of: $4i$ $-4i$

$$-6i$$

$$6i$$

$$4 - 6i$$

$$4 + 6i$$

$$4 + 6i$$

$$4 - 6i$$

$$-4 + 6i$$

$$-4 - 6i$$

ex. Write the polynomial with the following roots: 3, 4, $2i$, $-2i$

$$\begin{aligned}
 x &= 3 & x &= 4 & x &= 2i & x &= -2i \\
 x-3 &= 0 & x-4 &= 0 & x-2i &= 0 & x+2i &= 0 \\
 (x-3)(x-4)(x-2i)(x+2i) &= 0 \\
 (x^2 - 7x + 12)(x^2 + 4) &= 0 \\
 x^4 - 7x^3 + \underbrace{12x^2 + 4x^2}_{16x^2} - 28x + 48 &= 0 \\
 f(x) = x^4 - 7x^3 + 16x^2 - 28x + 48 &\gg 0
 \end{aligned}$$

ex. Find a polynomial from given zeros.

$$\begin{aligned}
 &-3, 4, 2-i, 2+i \\
 &(x+3)(x-4)(x-(2-i))(x-(2+i)) \\
 &(x+3)(x-4)(x-2+i)(x-2-i) \\
 &(x^2 - x - 12)(x^2 - 2x + i\cancel{x} - 2x + 4 + 2i + i\cancel{x} - 2i - i^2) \\
 &(x^2 - x - 12)(x^2 - 4x + 5) \\
 &x^4 - 4x^3 + 5x^2 - x^3 + 4x^2 - 5x - 12x^2 + 48x - 60 \\
 &x^4 - 5x^3 - 3x^2 + 43x - 60
 \end{aligned}$$

$$\text{Multiply: } (x - (6 - i))(x - (6 + i))$$

$$x^2 - 12x + 37$$

$$(x - (4 - i))(x - (4 + i))$$

$$x^2 - 8x + 17$$

$$(x - (3 + i))(x - (3 - i))$$

$$x^2 - 6x + 10$$

Factoring:

If odd degree, at least 1 real root.

$$f(x) = x^5 - 3x^4 - 5x^3 + 5x^2 - 6x + 8 \quad \frac{P}{Q} = \frac{\text{factors of 8}}{\text{factors of 1}}$$

$$\begin{array}{r} 4 \Big| 1x^5 - 3x^4 - 5x^3 + 5x^2 - 6x + 8 \\ \quad 4 \quad 4 \quad -4 \quad 4 \quad -8 \\ \hline 1 \Big| x^4 \quad 1 \quad -1 \quad 1 \quad -2 \quad |0 \\ \quad 1 \quad 2 \quad 1 \quad 2 \\ \hline -2 \Big| x^3 \quad 2 \quad 1 \quad 2 \quad |0 \\ \quad -2 \quad 0 \quad -2 \\ \hline \end{array} \quad \begin{array}{l} = \pm 1, 2, 4, 8 \\ \hline 1 \\ = \pm 1, 2, 4, 8 \end{array}$$

$$\begin{array}{r} 1 \Big| x^4 \quad 1 \quad -1 \quad 1 \quad -2 \quad |0 \\ \quad 1 \quad 2 \quad 1 \quad 2 \\ \hline -2 \Big| x^3 \quad 2 \quad 1 \quad 2 \quad |0 \\ \quad -2 \quad 0 \quad -2 \\ \hline \end{array} \quad \boxed{\text{Roots: } 4, 1, -2, i, -i}$$

$$\begin{array}{r} -2 \Big| x^2 \quad 0 \quad 1 \quad |0 \\ \quad -2 \quad 0 \quad -2 \\ \hline \end{array}$$

$$x^2 + 1 = 0$$

$$x^2 = -1$$

$$x = \pm i$$

Assignment
Mathlab Sec 2.5 day 2